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# Hybrid generative/discriminative classifier for unconstrained character recognition

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#### 9 Abstract

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10 Handwriting recognition for hand-held devices like PDAs requires very accurate and adaptive classifiers. It is such a 11 complex classification problem that it is quite usual now to make co-operate several classification methods. In this 12 paper, we present an original two stages recognizer. The first stage is a model-based classifier which store an exhaustive 13 set of character models. The second stage is a pairwise classifier which separate the most ambiguous pairs of classes. 14 This hybrid architecture is based on the idea that the correct class almost systematically belongs to the two more rel-15 evant classes found by the first classifier. Experiments on a 80,000 examples database show a 30% improvement on a 62 16 classes recognition problem. Moreover, we show experimentally that such an architecture suits perfectly for incremental 17 classification.

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19 Keywords: Handwriting recognition; Multiple classifier system; Pairwise neural networks; Confusion matrix; Adaptive classifier

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## 21 1. Introduction

Recently, hand-held devices like PDAs, mobiles
phones or e-books have became very popular. In
opposition to classical personal computers, they
are very small, keyboard-less and mouse-less.

Therefore, electronic pen is very attractive as26pointing and handwriting device. The first applica-27tion belongs to man-machine interface and the sec-28ond to handwriting recognition. Here, we focus on29the second one.30

For such an application, recognition rates 31 should be very high otherwise it should discourage 32 all the possible users. The major problem is the 33 vast variation in personal writing style. This problem can be solved either by constraining the al-

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lowed style of writing (PDA's *grafiti* alphabet: Fig.
la), trying to learn all personal writing styles (natural and script writing: Fig. 1b and c) to build an
omni-writer recognizer or building a mono-writer
recognizer by adapting the system to its user' style
and habits (abbreviations, mathematical or chemical symbols for scientists...).

In dynamic handwriting recognition, signal is 43 44 represented by sequences of (x, y) coordinates of 45 the pen moving. Each handwriting style has got 46 its typical allographs. This notion, particular to 47 handwriting, includes on the one hand characters having the same image but presenting a very vari-48 able dynamics in term of the number of stroke 49 50 composing the character, their senses and direction 51 and on the other hand, the different handwriting 52 model of a given character: cursive, hand-printed, 53 mixed...

54 Focusing on classification errors, there are two 55 situations which reduce the recognition rate.

Pattern might be unrelated to the training data.
As each user has his own way of writing, many dynamics can appear (Fig. 2a) This problem can be overcome by classifying both dynamic and static representations of the character and combining the classification results as shown in (Prevost and Milgram, 1997).

Pattern might be ambiguous (Fig. 2b) and some specific pairs of classes constitute the majority of errors made by the classifier like (B,D) or (7,1).

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The idea of our hybrid combination method is based on the fact that a given classifier can achieve very good performances in terms of correct recognition rate when considering the two more relevant



Fig. 1. Handwriting styles. (a) Constraint writing, (b) script writing, (c) natural writing.



Fig. 2. Ambiguous characters. (a) Unknown dynamics, (b) ambiguous characters.

classes (see Table 2). This observation motivates 72 the search for a suitable method which can detect 73 74 the correct classification among these two classes. This choice results in a two class (binary) problem. 75 76 In this paper, we explore the following combination scheme. First stage generative classifier is used 77 to detect ambiguous pairs of classes and the sec-78 ond stage is discriminative. It is composed of a 79 set of pairwise neural networks, one for each 80 ambiguous pair of classes. 81

The paper is organized as follows. Section 2 de-82 scribes several standardized methods used for 83 character classification and ways to build two 84 stage classifier well-known for their accuracy. Sec-85 tion 3 details the first stage model-based classifier. 86 Section 4 is devoted to the implementation of the 87 second stage discriminative classifier used to im-88 prove performances. In Section 5, we show that 89 this hybrid approach is adaptive. Finally, conclud-90 ing remarks and future works are discussed in Sec-91 tion 6. 92

## 2. Review of classification methods 93

### 2.1. Model generation vs discrimination 94

There are two standard ways to perform handwriting classification: generate models (to build the so-called model-based classifier) or discriminate. 97

Generative classifiers train one (or several) 98 model(s) for each character class with examples 99 of this single class. During the test stage, the classification is performed according to similarity between the unknown pattern and the models. 102 Neural models (Schwenk and Milgram, 1996), 103

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104 Markovian models (Connell and Jain, 1999) or prototype-based models (Anquetil and Lorette, 105 1996; Prevost and Milgram, 2000; Vuori et al., 106 2002) are usual to perform handwriting recogni-107 108 tion (Plamondon and Srihari, 2000). All these 109 models are perfectly fitted to multi-modal classes 110 and can face the variability of handwriting. Their main drawback is the possibility of model overlap-111 112 ping when classes are ambiguous (Fig. 3a).

113 Discriminative classifiers find optimal frontiers 114 between classes (Fig. 3b). These classifiers are 115 trained using examples of a given set of classes 116 (two, or more). Guyon et al. (1991) use a single 117 network to perform discrimination. Oh and Suen (2002) apply a "class-modular" (also called "one 118 119 against all") strategy and train N networks. Each 120 classifier is trained to discriminate one class from 121 all the remaining classes (N-1). They show that 122 this approach is more accurate than the single net-123 work approach, especially when the number of 124 class increases. Another method is the "pairwise 125 coupling", which consists to construct a classifier 126 for each pair of classes. Thus, a N class problem 127 is decomposing in N(N-1)/2 binary sub-prob-128 lems. Price et al. (1994) train pairwise neural net-129 works (the so called PNN) to separate pairs of 130 classes (for a N-classes problem). Such a solution 131 seems really promising because it reduces the N-132 classes problem to two-classes problems. But it is 133 not so relevant when N increases. For example, 134 in the capital letters case, it leads to 325 PNN's cre-135 ation. The question is: is it necessary to train a discriminative classifier when data can be easily 136 137 discriminated? and, in such a case, should a mod-138 el-based classifier be sufficient?

139 Comparing both approaches, it seems relevant 140 to build a hybrid recognizer to obtain the best of



Fig. 3. Generative classifier (a) and discriminative classifier (b).

both words (Raina et al., 2003). Teo and Shinghal 141 142 (1997) combine a ruled-based classifier with PNN to confirm or reject data. OCR applications are 143 also presented by Avi-Itzhak et al. (1995) and 144 Wang and Jean (1993) to solve multifont character 145 recognition and confusions with hierarchical NN. 146 In our approach, a model-based classifier find the 147 most relevant pair of classes. Then, PNN are used 148 to improve significantly the accuracy of the model-149 based classifier in local areas around the frontiers 150 between each pair of ambiguous classes. 151

#### 2.2. Two stage classification 152

As shown before, the reason why handwriting 153 recognition is so difficult is the huge style variation 154 and variability in handwriting, leading to the con-155 clusion that a single classifier cannot recognize all 156 kinds of handwriting. The combination of different 157 classifiers, trained on distinct features and/or dif-158 159 ferent data has been applied successfully on handwriting recognition as discussed in recent reviews 160 (Jain et al., 2000; Rahman and Fairhust, 2003). 161 Here, we focus on a particular combination 162 scheme: the two stage classifier. In his taxonomy, 163 Rahman describes the multi-stage classifier as a 164 vertical decision combination where "at each stage 165 there is only one classifier operating and process-166 ing the patterns". The class set reduction approach 167 is one of the basic strategy to deal with such a 168 combination. At each stage, the classifier generates 169 a list of the set of possible classes the current char-170 acter might belong. The next classifier limits fur-171 ther investigations to this subset and produces a 172 reduced list and so on. 173

174 Bellili et al. (2003) developed an hybrid MLP-SVM classifier. The first stage is a single neural 175 network (MLP). Ambiguous character pairs are 176 found by computing its confusion matrix and esti-177 mating the error probability for each pair. The sec-178 ond stage is a set of local, pairwise SVMs (one for 179 each ambiguous pairs) tuned to detect the correct 180 class among the MLP's two maximum output. 181 Mark that both stages are discriminative. Milgram 182 et al. (in press) pre-estimates probabilities in the 183 184 first stage with a model-based approach an re-estimates only the highest probabilities with appropri-185 ate SVM in the second stage. The author try to get 186

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187 the best of both generative and discriminative classifiers. In (Vuurpijl et al., 2003), several ways to de-188 tect conflicts in any first stage classifier or 189 ensemble of classifiers are described. Majority vote 190 191 is explored, to activate pairwise SVM again. In 192 fact, these two stage classifiers can be seen as par-193 ticular extension of the probabilistic AdaBoost 194 (Freund and Schapire, 1997), where two classifiers 195 are tuned on different training sets. The second 196 stage training set depends on the performances of the first one and the second stage classifier (or 197 198 ensemble of classifiers) focuses on local areas 199 around the frontiers between ambiguous classes.

#### 200 3. Model-based classifier

#### 201 3.1. Prototype-based recognition system

The recognition system used in the experiments is based on prototype matching. It consists of a prototype set covering several writing styles, a dissimilarity measure used for comparing input characters and prototypes, and a decision rule according to which classifications are carried out (Fig. 4).

209 The prototype set was built using the MDCA 210 clustering algorithm described in (Prevost and Milgram, 2000). This algorithm is divided into two 211 212 stages. The agglomeration stage gathers references 213 around prototypes according to an index of prox-214 imity provided by the analysis of inter-reference 215 distance matrix. The adaptation stage optimizes 216 the prototypes and thus improves the character models. Thus, each character model is composed 217 218 of a set of prototypes.



Fig. 4. Model-based classifier.

The nearest neighbor rule is used as the classifi-219 cation criterion. The distance between the input 220 character and each prototype is computed by dy-221 namic programming. Then for each class, the 222 smallest distance is retained, giving a distance vec-223 tor  $\boldsymbol{D} = (D_1, D_2, \dots, D_N)$ . Assuming that distances 224 are normally distributed (one distribution per 225 class, parameters:  $m_i$ ,  $\sigma_i$  estimated on the reference 226 dataset), we can compute a posterior probability 227 vector  $\mathbf{p} = (p_1, p_2, \dots, p_N)$  and find the most rele-228 vant class and the second one. 229

 $C_1 = \operatorname{argmax1}(\boldsymbol{p})$   $C_2 = \operatorname{argmax2}(\boldsymbol{p})$ 

#### 3.2. Database, pre-processing and results 232

233 Experiments have been carried out on the Unipen dataset Train R01-V07 initiated by Guyon et 234 al. (1994), artificially divided into three subsets 235 (Table 1), namely the training set  $S_{\text{TR}}$  (used for 236 clustering), the cross-validation set  $S_{CV}$  and the 237 testing set  $S_{\text{TE}}$ . Characters are simply pre-pro-238 239 cessed. The sequence of (x, y)-coordinates is resampled with 20 points per stroke, centered 240 and normalized in (-1,1) preserving the aspect 241 242 ratio.

Table 2 gives the size of the prototype set  $S_{\text{proto}}$ 243after clustering and the recognition rates on the244test set considering the correct class is respectively245the first answer (top 1) or one of the two best an-246swers (top 2). It shows the robustness of the recog-247nizer and validates our first assumption: finding an248

Table 1 Data-sets

	$S_{\mathrm{TR}}$	$S_{\mathrm{TE}}$	$S_{\rm CV}$
Digit	8000	4000	2000
Uppercase	12,826	6355	3188
Lowercase	23,922	11,443	5974

Table 2

Model-based classifier: size of the prototype set and recognition rates (test set  $S_{TE}$ )

	$S_{\rm proto}$	Top 1 (%)	Top 2 (%)
Digit	476	98.9	99.8
Uppercase	1158	96.7	99.0
Lowercase	1114	96.3	98.8

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249 adequate method to detect confusion among the 250 first and second most relevant classes should in-251 crease greatly the system accuracy.

#### 252 4. Hybrid classifier

#### 253 4.1. PNN training process

254 The model-based classifier generates a probabil-255 ity vector. The first and second higher probabilities 256 indicate the first and second most relevant class 257  $(C_1 \text{ and } C_2)$ . One pairwise neural network can be 258 trained to separate these two classes and detects the most relevant one. Under the assumption that, 259 first, the behavior of the classifier is characterized 260 261 by a confusion matrix and, second, that its prior behavior is representative of its posterior behavior, 262 the pairs of ambiguous classes (i, j) can be easily 263 264 detected. The confusion matrix is computed on the digit training set  $S_{\text{TR}}$  (Fig. 5). As we focus 265 266 on confusions, the diagonal (which indicates cor-267 rect classifications) is set to zero and the number of confusions  $N_{i|i}$  for each pair of classes can be 268 computed by summing the number of confusions 269 for both pairs (i, j) and (j, i). 270

- 271 We can make three observations:
- many pairs of classes are not ambiguous: training PNN for these pairs of classes is useless;



- some other pairs are slightly ambiguous: training PNN for these pairs can be useful; 275
- some pairs cause the majority of confusions: for 276 example (1,7), (3,7) or (4,9). These pairs need 277 to be discriminated. 278

So, a confusion threshold  $\delta_{conf}$  can be used to adjust the number of PNN created and, by the way, the accuracy and speed of the hybrid recognizer. 280

Given the confusion matrix  $M_{conf}$  on the training set  $S_{TR}$ , and the number of confusions for each pair  $N_{i/j}$ , we can compute the total number of confusions  $N_{tot}$  and the confusion probability  $p_{i/j}$ : 287

$$N_{ ext{tot}} = \sum_{i} \sum_{j} N_{i/j} \quad p(i,j) = rac{N_{i/j}}{N_{ ext{tot}}}$$

We can choose to take into account the most 290 frequent confusions (for which the confusion 291 probability is the highest) i.e. confusions for 292 which: 293

$$p(i,j) > \frac{p_{\max}}{\delta_{\text{conf}}}$$
 where  $p_{\max} = \max\{p(i,j)\}$ 

Table 3 specifies the set of ambiguous pairs (i, j)296detected for digits for a given threshold  $\delta_{conf}$ . This297set is denoted298

$$S_{\delta_{ ext{conf}}} = \left\{ (i, j) \left| p(i, j) > \frac{p_{\max}}{\delta_{ ext{conf}}} \right\} 
ight.$$

 Table 3

 Ambiguous digit pairs vs confusion threshold

$\overline{S_2}$	$S_4$	$S_6$	$S_8$	$S_{10}$
1,2	1,2	1,2	1,2	1,2
1,7	1,7	1,3	1,3	1,3
1,9	1,9	1,4	1,4	1,4
3,7	2,7	1,5	1,5	1,5
	3,7	1,7	1,7	1,7
	4,9	1,9	1,9	1,9
	5,9	2,7	2,7	2,7
	7,9	3,7	3,7	3,7
		3,0	3,0	3,0
		4,7	4,7	4,7
		4,9	4,9	4,9
		5,9	5,9	5,9
		6,0	6,0	6,0
		7,9	7,9	7,9
		8,0	8,0	8,0

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301 For these ambiguous pairs (i, j), a PNN is 302 trained. This is a binary classification problem: i 303 will be associated to the PNN label +1 and *j* will 304 be associated to the other label -1. In Table 4, 305 we give the number of PNN created for digits, 306 uppercase and lowercase letters for each confusion 307 threshold. For  $\delta_{conf} = 10$ , we train no more than 112 PNN. If we try to separate every pairs of clas-308 309 ses (even considering separately digits, uppercase and lowercase letters) there should be some 695 310 311 PNN.

#### 312 4.2. Hybrid classification process

313 For an unknown (unlabelled) pattern of the test 314 set  $S_{\text{TE}}$ , two situations can be observed. If the pair 315  $(C_1, C_2)$  does not belong to  $S_{\delta_{\text{conf}}}$ , then we keep the model-based classifier output  $C_1$ . Else, an ambigu-316 317 ity threshold  $\delta_{amb}$  is defined and used to activate 318 the PNN. Given the posterior probabilities for 319 the two most relevant classes  $p_{C_1}$  and  $p_{C_2}$ , we con-320 sider that the model-based classifier output is 321 ambiguous when:  $\Delta p = p_{C_1} - p_{C_2} < \delta_{amb}$ .

322 Then, PNN  $(C_1, C_2)$  is activated. There are two 323 extrema:

324	• $\delta_{amb} = 0$ : PNN is inhibited and the model-based
325	classifier works alone.

- 326  $\delta_{amb} = 1$ : PNN is always activated when a confusion ( $C_1, C_2$ ) is detected.
- 328

329 We show (Fig. 6) the PNN activation rate 330 which obviously increases when  $\delta_{amb}$  does.

#### 331 4.3. Database, pre-processings and results

The original training sets for each ambiguous pair (i,j) do not have the same size and the number of confusions is small. So the frontier between *i* 

Table 4 PNN number vs confusion threshold					
$\delta_{\rm conf}$	2	4	6	8	10
Digit	4	8	15	15	15
Uppercase	4	14	18	24	48
Lowercase	9	18	27	39	49
Total	17	40	50	78	112



Fig. 6. PNN activation rate vs ambiguity and confusion thresholds.

and j is not well defined and the corresponding335PNN cannot generalize correctly (Table 5). Confusions on the training set were detected and their336number was artificially increased by transforming338them: each confusion generates new examples339slightly expanded, contracted or rotated. So, a340modified training set  $S'_{TR}$  is generated.341

Characters confused by the model-based classifier have always the same number of strokes. In order to get input vectors of the same size, characters are re-sampled to 20 points.

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PNN are completely connected multi-layer per-346 ceptron and have the following architecture: 40 347 cells on the input layer corresponding to the 20 348 (x, y)-coordinates, one hidden layer and one out-349 put cell. PNN are trained using the back-propaga-350 tion algorithm on the modified training set  $S'_{TR}$ 351 and training is stopped on cross-validation set 352  $S_{\rm CV}$ . Several trainings have been done to optimize 353 the hidden layer size and 10 hidden cells achieve 354 the best recognition rate (Table 5). This latter is 355 slightly better when using the modified training 356 set. 357

Table 5				
PNN recog	nition rates	on the	test s	et $(S_{\text{TE}})$

	Original training set (%)	Modified training set (%)
Digit	99.7	99.6
Uppercase	99.1	99.3
Lowercase	98.8	99.5

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358 We tested our hybrid recognizer on the test set 359  $(S_{\text{TE}}: 21,800 \text{ examples})$ . The following Figs. 7–9 360 summarize the system performances on digits, uppercase and lowercase letters. We can observe 361 that the recognition rate increases when the confu-362 363 sion threshold  $\delta_{conf}$  does (except for digits, but the 364 number of examples involved is to small to come to a conclusion). The second observation is that 365 the recognition rate increases in a quasi-monoto-366 nous way when the ambiguity threshold  $\delta_{amb}$  does, 367 368 higher than the model-based classifier rate. Final-369 ly, Table 6 summarizes the best performances 370 (with  $\delta_{conf} = 10$  and  $\delta_{amb} = 1$ ) of the hybrid classi-371 fier compared with the original model-based classifier. These results prove that our hybrid recognizer 372



Fig. 7. Hybrid classifier recognition rates on digits vs ambiguity and confusion thresholds (test set  $S_{TE}$ ).



Fig. 8. Hybrid classifier recognition rates on uppercase vs ambiguity and confusion thresholds (test set  $S_{TE}$ ).



Fig. 9. Hybrid classifier recognition rates on lowercase vs ambiguity and confusion thresholds (test set  $S_{TE}$ ).

Table 6 Hybrid classifier: recognition rates (test set  $S_{\text{TE}}$ )

	Model-based classifier (%)	Hybrid classifier (%)
Digit	98.9	99.1
Uppercase	96.7	97.9
Lowercase	96.3	97.8

increases significantly the performances in terms of 373 recognition rate for on-line handwriting 374 classification. 375

#### 5. Adaptive classifier

In this section, we try to show that our hybrid recognizer is perfectly suited for adaptive learning i.e. can support the addition of new classes. This preliminary study is just a simulation: we consider that the former classifier just recognized 26 uppercase letters and we try to add 10 new classes corresponding to digits. 377 378 379 380 380 381 382 383

#### 5.1. Adapting the model-based classifier 384

Thanks to its structure, the model-based classifier can easily be adapted to including new classes. 386 In opposite to discriminative classifiers (which need a complete re-training), generative classifiers 388 are naturally incremental as model for one class is trained with data of this sole class. Once trained, 390 the new models are included in the classifier and 391

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- 392 the decision is taken considering the former and 393 the new models (Fig. 10).
- 394 5.2. Adapting the hybrid classifier
- 395 The adaptation is made as follows:
- 396 (1) The extended confusion matrix including all397 the 36 classes is computed on the training
- 398 set. As we can see (Fig. 11) cross-confusions 399 between uppercase letters and digits like 400 (O,0), (I,1), (S,5) and (Z,2) are obviously



Fig. 10. Adapted model-based classifier.



Fig. 11. Extended confusion matrix (uppercase letters and digits: training set  $S_{\text{TR}}$ ).

numerous. In context-free recognition, this401kind of confusions cannot be found. So, we402choose to delete these latter and zoom-up403on cross-confusions (Fig. 12).404

- (2) Confusions between former classes and new classes (the so-called cross-confusions) are detected, using a confusion threshold  $\delta_{conf} = 10$ .
- (3) Corresponding PNN are trained.

Table 7 shows the recognition rates in the fol-410lowing cases:412

- Model-based classifier alone: recognition rate 413 falls dramatically owing to cross-confusions 414 between uppercase letters and digits like (O,0), 415 (I, 1), (S, 5) and (Z, 2) for example. 416
- Former hybrid classifier: confusions between 417 uppercase letters (U,U) and digits (D,D) are 418 considered but cross-confusions are ignored. 419
- Adapted hybrid classifier: all the confusions 420 including cross-confusions (U, D) are taken into 421 account. The result is impressive: the error rate 422 has been reduced by half when compared with the former model-based classifier. PNN have focused on local features to discriminate confusive 425 sive characters. 426



Fig. 12. Cross-confusions (uppercase letters (1–26) and digits (27–36)).

Table /								
Adapted	hybrid	classifier:	recognition	rates	(test	set	$S_{\text{TE}}$ )	and
PNN nui	nber							

Model-based classifier	Model-based	Hybrid classifier		
	(U,U) $(D,D)$	(U,U) $(D,D)$ $(U,D)$		
Reco. rate PNN	90.3% -	91.5% 63	95.4% 79	

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#### 429 6. Conclusions

430 The main idea of this paper is that the recogni-431 tion process can be performed in two stages. The 432 first classifier is a competition between all classes 433 and just leads to "happy fews" (2 for instance) 434 selected classes. This kind of "short list" cannot 435 be just processed by a competition between several 436 models but needs discrimination. The reason is 437 that remaining ambiguity is concentrated in very 438 specific and local features (think to the differ-439 ence between uppercase B and D). If data are 440 available, they can be used to determine cases 441 where mistakes are made and train pairwise, local 442 classifiers.

443 Moreover, the proposed architecture suits per-444 fectly to incremental classification: contrary to dis-445 criminative classifiers, this combined generative-446 discriminative classifier can be adapted to new 447 classes without a complete retraining. It just need 448 to estimate the new models (generation step), 449 detecting cross-confusions and training the corre-450 sponding PNN.

451 We have recently designed a handwriting text 452 recognizer (Oudot et al., 2004) and the proposed 453 recognizer should be integrated into the system. 454 Nevertheless, a question remains: at the present 455 time, the second stage classifier uses a large data-

456 base to determine pairwise confusions and to train 457 the pairwise neural networks, what will be the train-

458 ing result on a small set of confused examples?

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